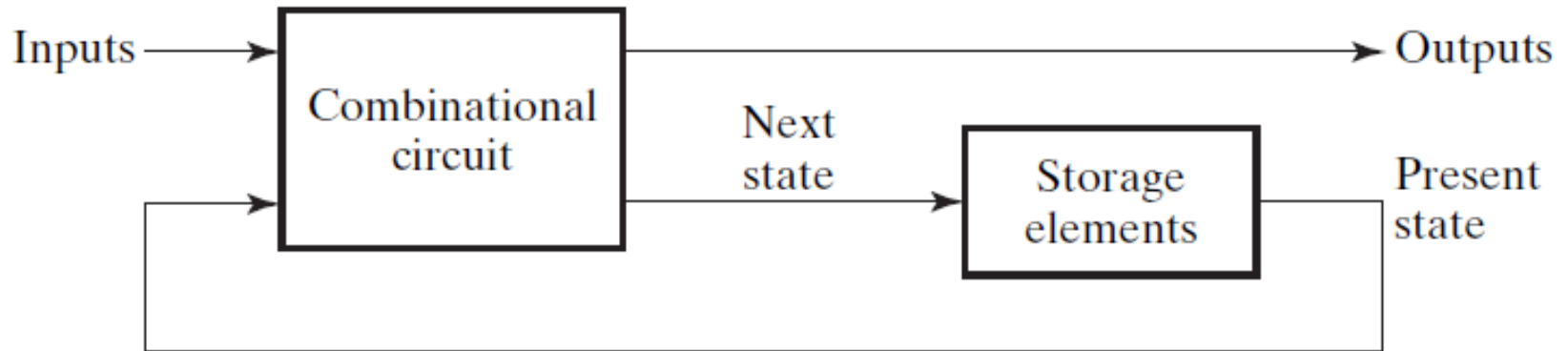
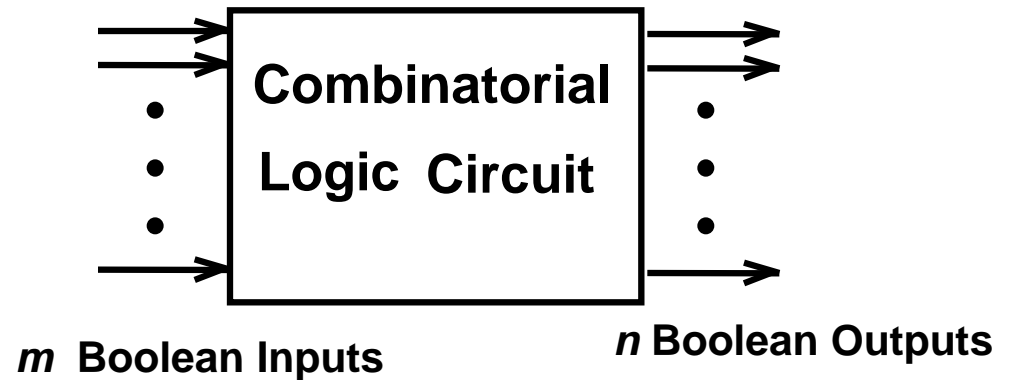

Counters and Registers

Dr. Anurag Srivastava

Basic of digital design

- Basic gates (AND ,OR, NOR, NAND and INVERTER)
- Universal gates (NAND and NOR)
- Design of any function using basic gates
- $F=xy+(xyz+zx+xz)xy$
- Truth table verification
- K-map for solving a complex functions
- Difference between the Combinational circuits and Sequential Circuits

Combinational functional blocks



Block of sequential

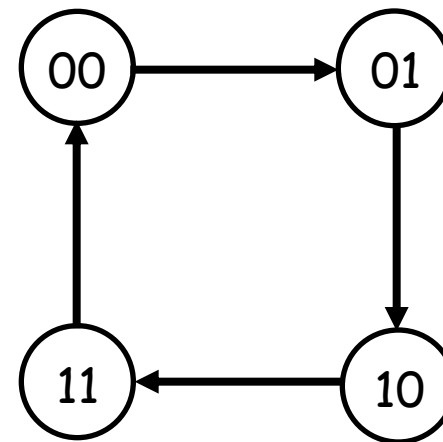
Introducing counters

- Counters are a specific type of sequential circuit
- The state serves as the "output" (Moore)
- A counter that follows the binary number sequence is called a binary counter
 - n-bit binary counter: n flip-flops, count in binary from 0 to 2^n-1
- Counters are available in two types:
 - Synchronous Counters
 - Ripple Counters
- Synchronous Counters:
 - A common clock signal is connected to the C input of each flip-flop

Synchronous Binary Up Counter

- The output value increases by one on each clock cycle
- After the largest value, the output “wraps around” back to 0
- Using two bits, we'd get something like this:

Present State		Next State	
A	B	A	B
0	0	0	1
0	1	1	0
1	0	1	1
1	1	0	0

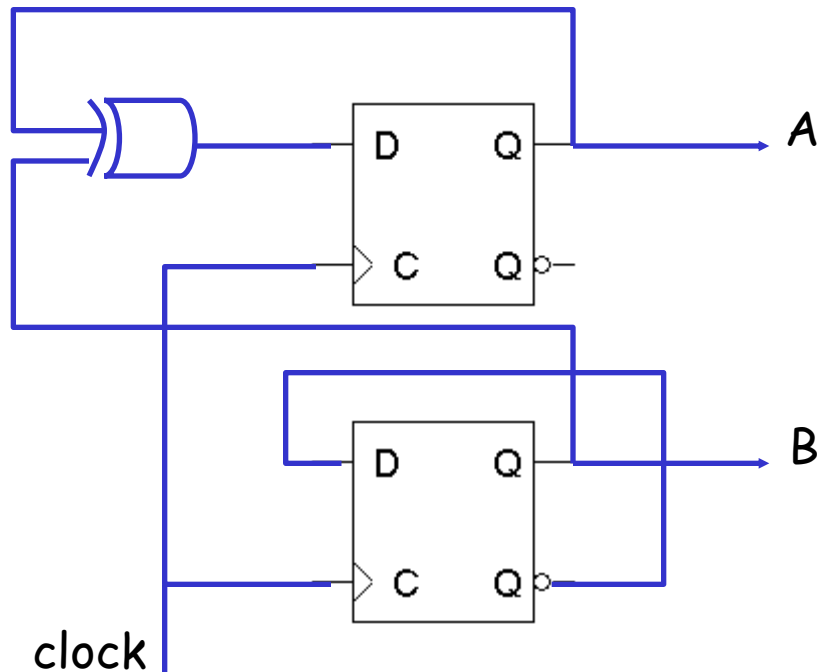


Synchronous Binary Up Counter

Present State		Next State	
A	B	A	B
0	0	0	1
0	1	1	0
1	0	1	1
1	1	0	0

$$D1 = A'B + AB'$$

$$D0 = B'$$



What good are counters?

- Counters can act as simple clocks to keep track of "time"
- You may need to record how many times something has happened
 - How many bits have been sent or received?
 - How many steps have been performed in some computation?
- All processors contain a **program counter**, or **PC**
 - Programs consist of a list of instructions that are to be executed one after another (for the most part)
 - The PC keeps track of the instruction currently being executed
 - The PC increments once on each clock cycle, and the next program instruction is then executed.

Synch Binary Up/Down Counter

- 2-bit Up/Down counter
 - Counter outputs will be 00, 01, 10 and 11
 - There is a single input, X.
 - > X= 0, the counter counts up
 - > X= 1, the counter counts down
- We'll need two flip-flops again. Here are the four possible states:

00

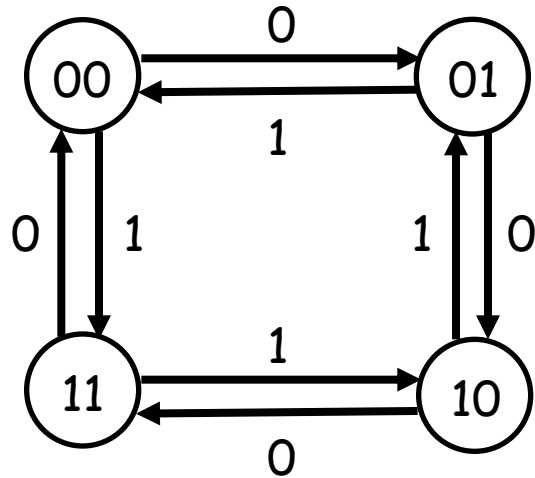
01

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10

The complete state diagram and table

- Here's the complete state diagram and state table for this circuit



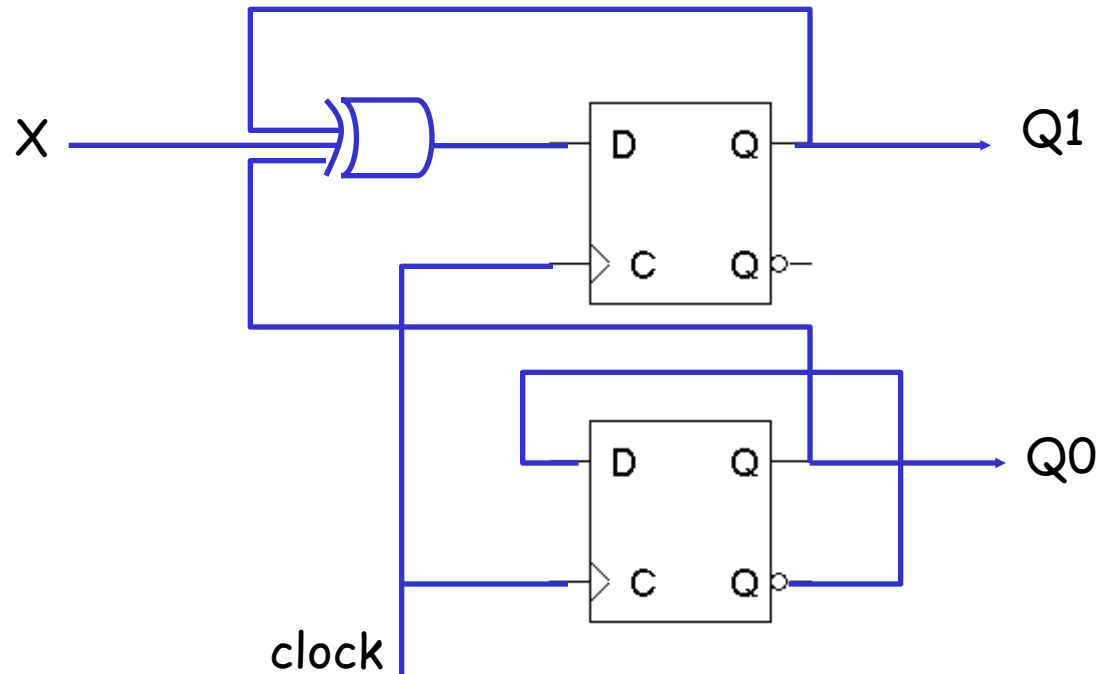
Present State		Inputs X	Next State	
Q ₁	Q ₀		Q ₁	Q ₀
0	0	0	0	1
0	0	1	1	1
0	1	0	1	0
0	1	1	0	0
1	0	0	1	1
1	0	1	0	1
1	1	0	0	0
1	1	1	1	0

- | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
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| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 | 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 | 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 | 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 | 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 | 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |
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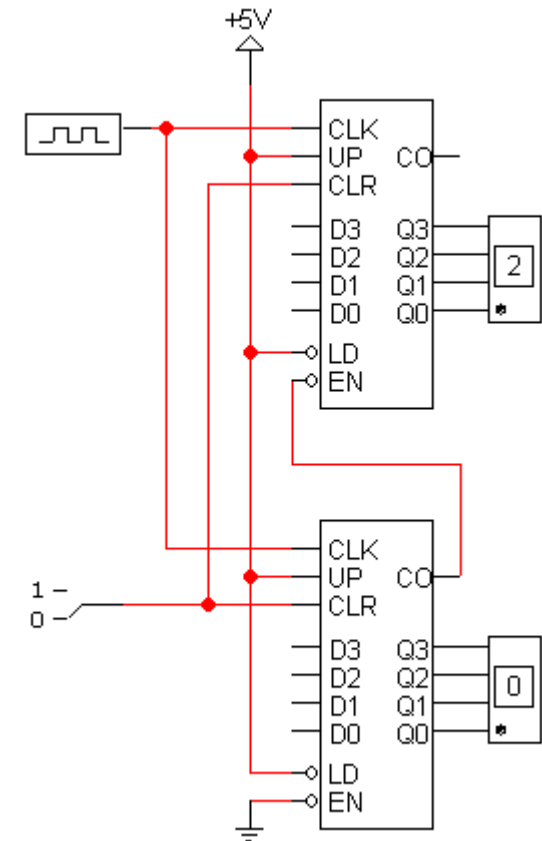
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Synchronous Binary Up/Down Counter

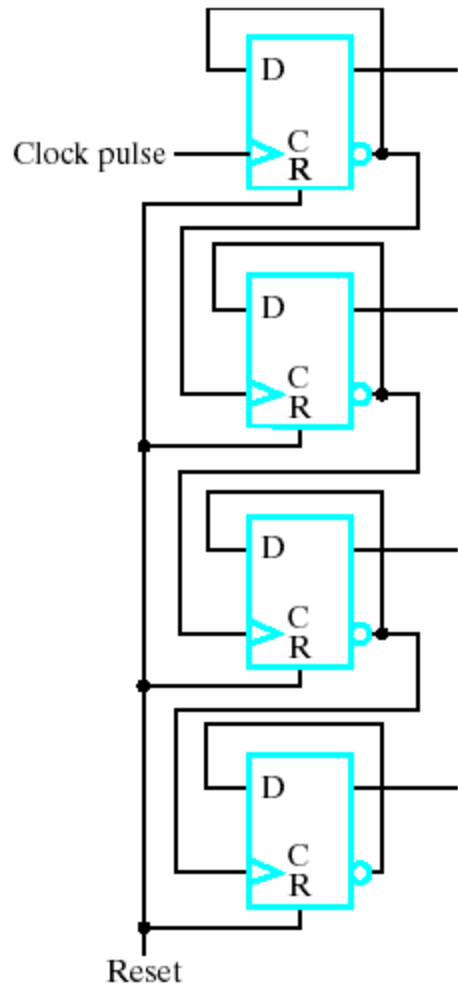


An 8-bit counter

- As you might expect by now, we can use these general counters to build other counters
- Here is an 8-bit counter made from two 4-bit counters
 - The bottom device represents the least significant four bits, while the top counter represents the most significant four bits
 - When the bottom counter reaches 1111 (i.e., when $CO = 0$), it enables the top counter for one cycle
- Other implementation notes:
 - The counters share clock and clear signals
 - Hex displays are used here



Ripple Counter



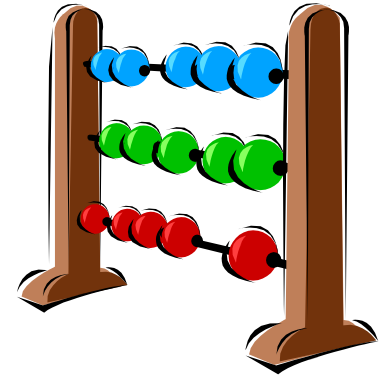
Upward Counting Sequence

Q_3	Q_2	Q_1	Q_0
0	0	0	0
0	0	0	1
0	0	1	0
0	0	1	1
0	1	0	0
0	1	0	1
0	1	1	0
0	1	1	1
1	0	0	0
1	0	0	1
1	0	1	0
1	0	1	1
1	1	0	0
1	1	0	1
1	1	1	0
1	1	1	1

Simple, yet asynchronous circuits !!!

Summary

- Counters serve many purposes in sequential logic design
- There are lots of variations on the basic counter
 - Some can increment or decrement
 - An enable signal can be added
 - The counter's value may be explicitly set
- There are also several ways to make counters
 - You can follow the sequential design principles to build counters from scratch
 - You could also modify or combine existing counter devices



Registers

- A common sequential device: Registers
 - They're a good example of sequential analysis and design
 - They are also frequently used in building larger sequential circuits
- **Registers** hold larger quantities of data than individual flip-flops
 - Registers are central to the design of modern processors
 - There are many different kinds of registers
 - We'll show some applications of these special registers

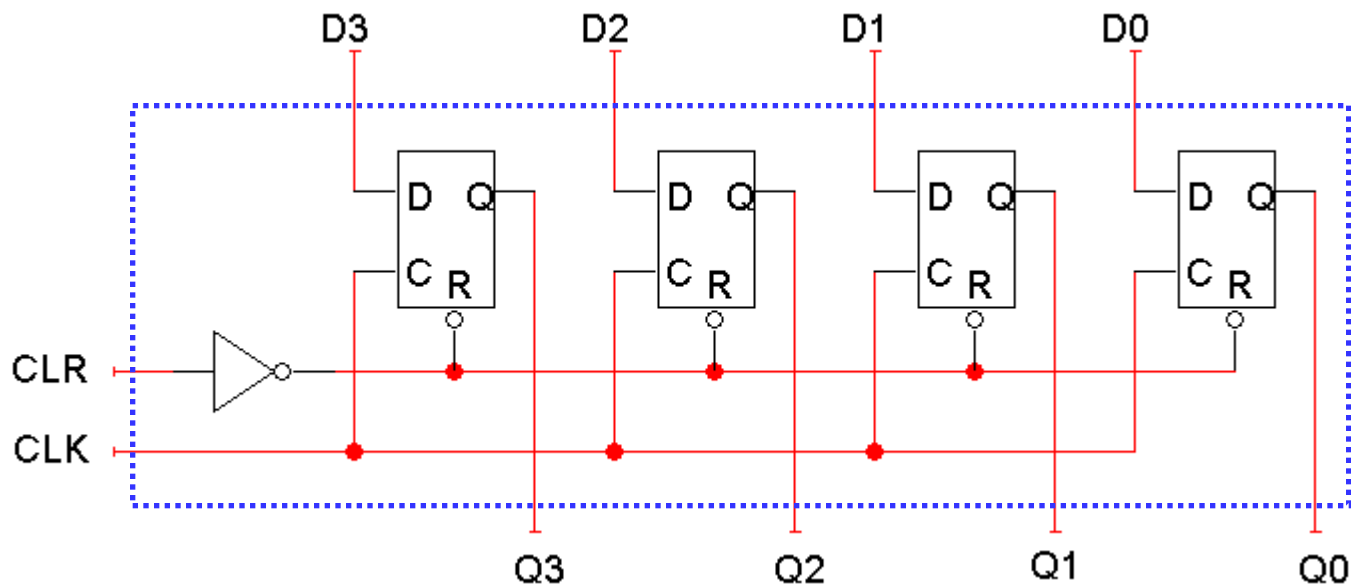


What good are registers?

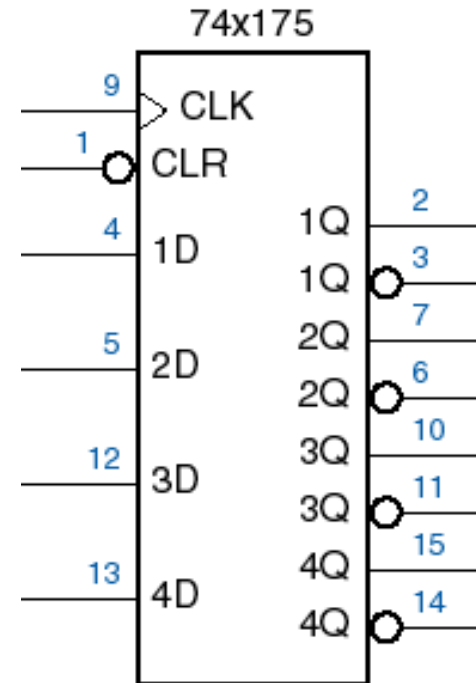
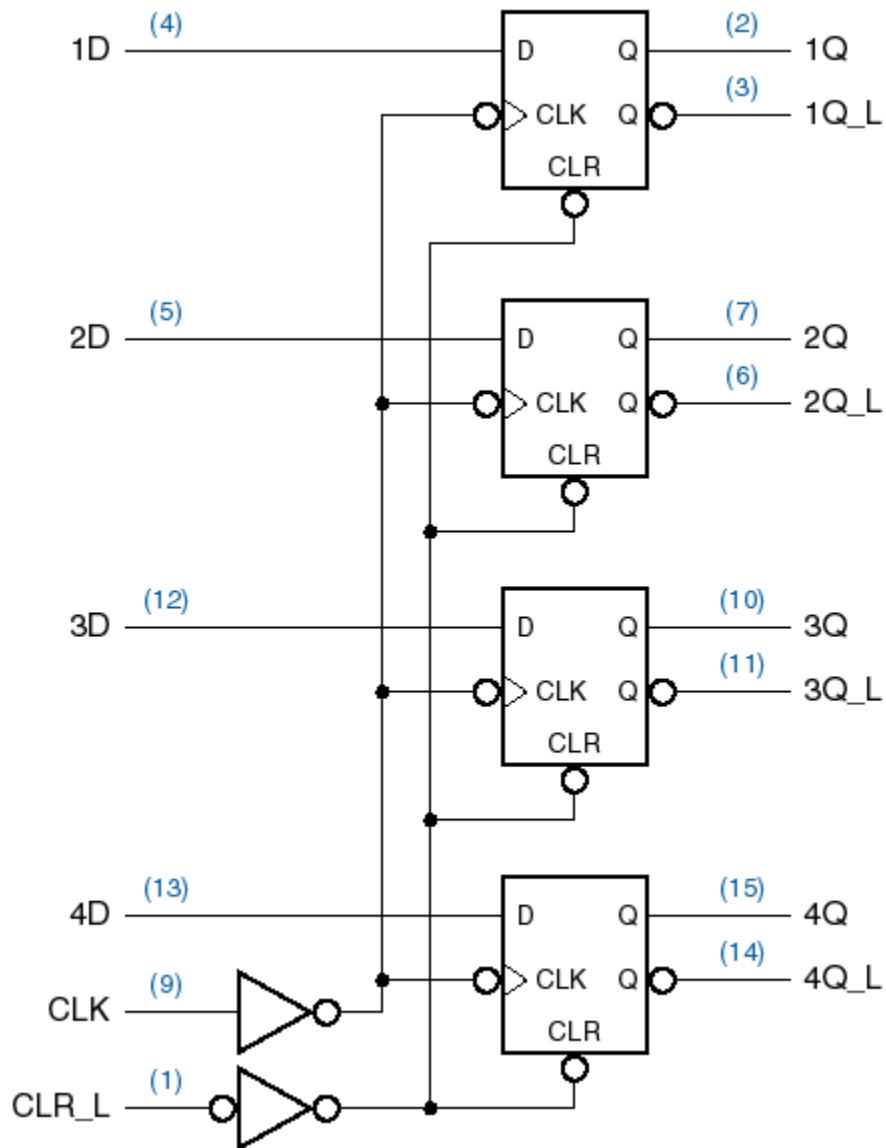
- Flip-flops are limited because they can store only one bit
 - We had to use two flip-flops for our two-bit counter examples
 - Most computers work with integers and single-precision floating-point numbers that are 32-bits long
- A **register** is an extension of a flip-flop that can store multiple bits
- Registers are commonly used as temporary storage in a processor
 - They are faster and more convenient than main memory
 - More registers can help speed up complex calculations

A basic register

- Basic registers are easy to build. We can store multiple bits just by putting a bunch of flip-flops together!
- A 4-bit register is given below
 - This register uses D flip-flops, so it's easy to store data without worrying about flip-flop input equations
 - All the flip-flops share a common **CLK** and **CLR** signal



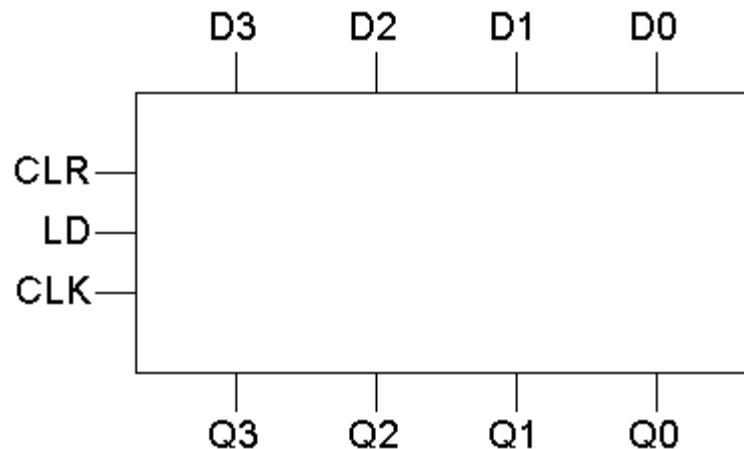
74x175 - 4-bit register



Adding a parallel load operation

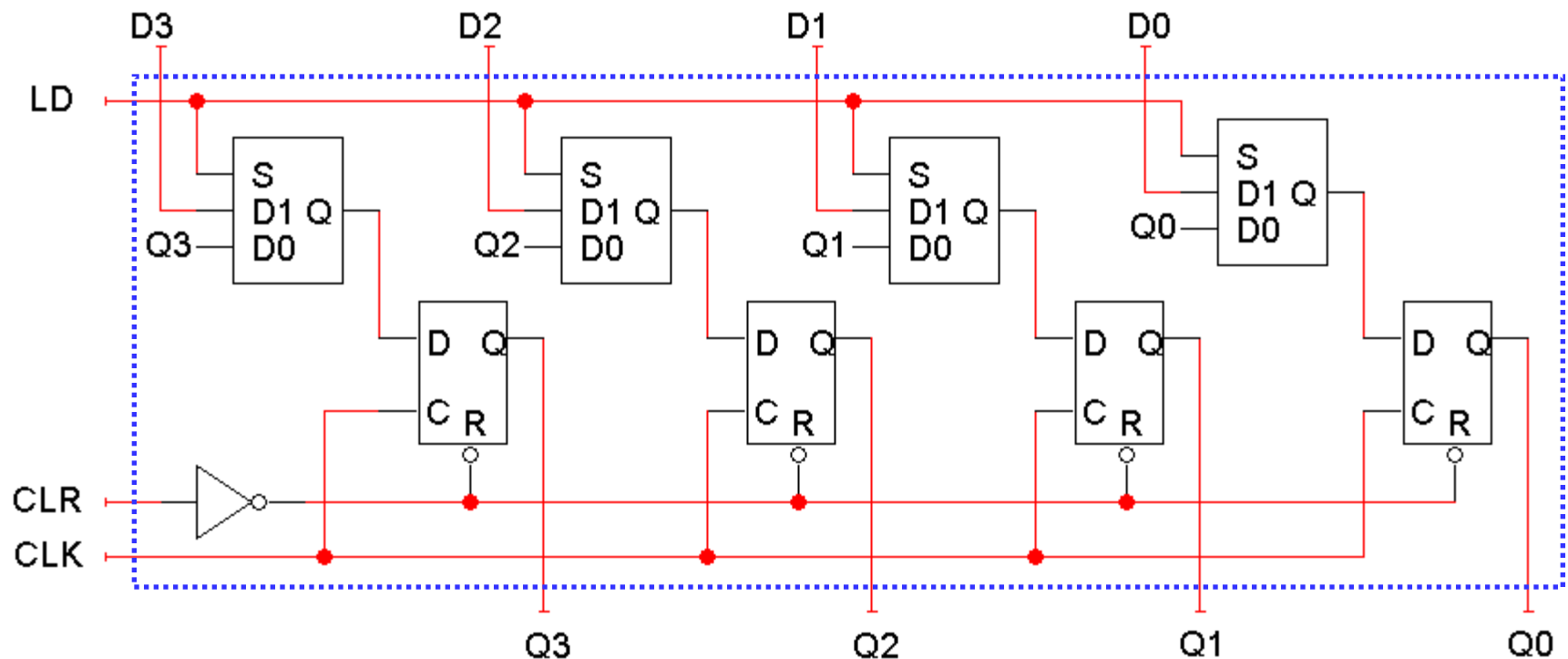
- The input D_3-D_0 is copied to the output Q_3-Q_0 on *every* clock cycle
- How can we store the current value for more than one cycle?
- Let's add a load input signal LD to the register
 - If $LD = 0$, the register keeps its current contents
 - If $LD = 1$, the register stores a new value, taken from inputs D_3-D_0

LD	$Q(t+1)$
0	$Q(t)$
1	D_3-D_0



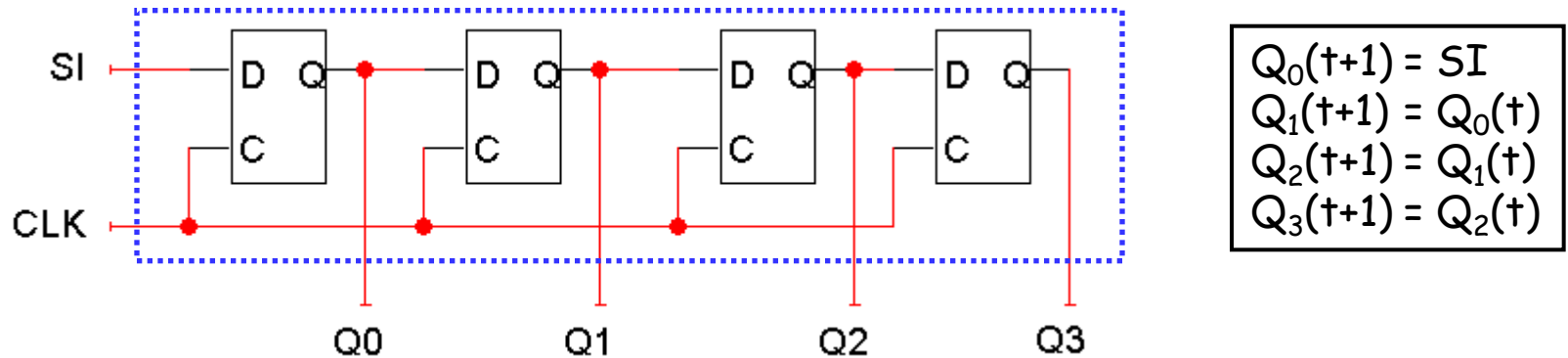
Register with parallel load

- When $LD = 0$, the flip-flop inputs are Q_3 - Q_0 , so each flip-flop just keeps its current value
- When $LD = 1$, the flip-flop inputs are D_3 - D_0 , and this new value is "loaded" into the register.



Shift Register

- A **shift register** "shifts" its output once every clock cycle.



- SI** is an input that supplies a new bit to shift "into" the register
- For example, if on some positive clock edge we have:

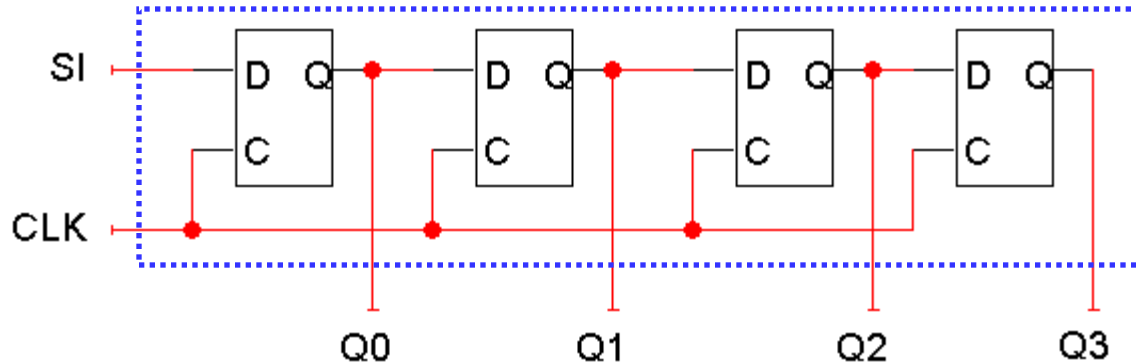
$$\begin{aligned} SI &= 1 \\ Q_0-Q_3 &= 0110 \end{aligned}$$

then the next state will be:

$$Q_0-Q_3 = 1011$$

- The current Q_3 (0 in this example) will be lost on the next cycle

Shift direction



$$\begin{aligned} Q_0(t+1) &= SI \\ Q_1(t+1) &= Q_0(t) \\ Q_2(t+1) &= Q_1(t) \\ Q_3(t+1) &= Q_2(t) \end{aligned}$$

- The circuit and example make it look like the register shifts "right."

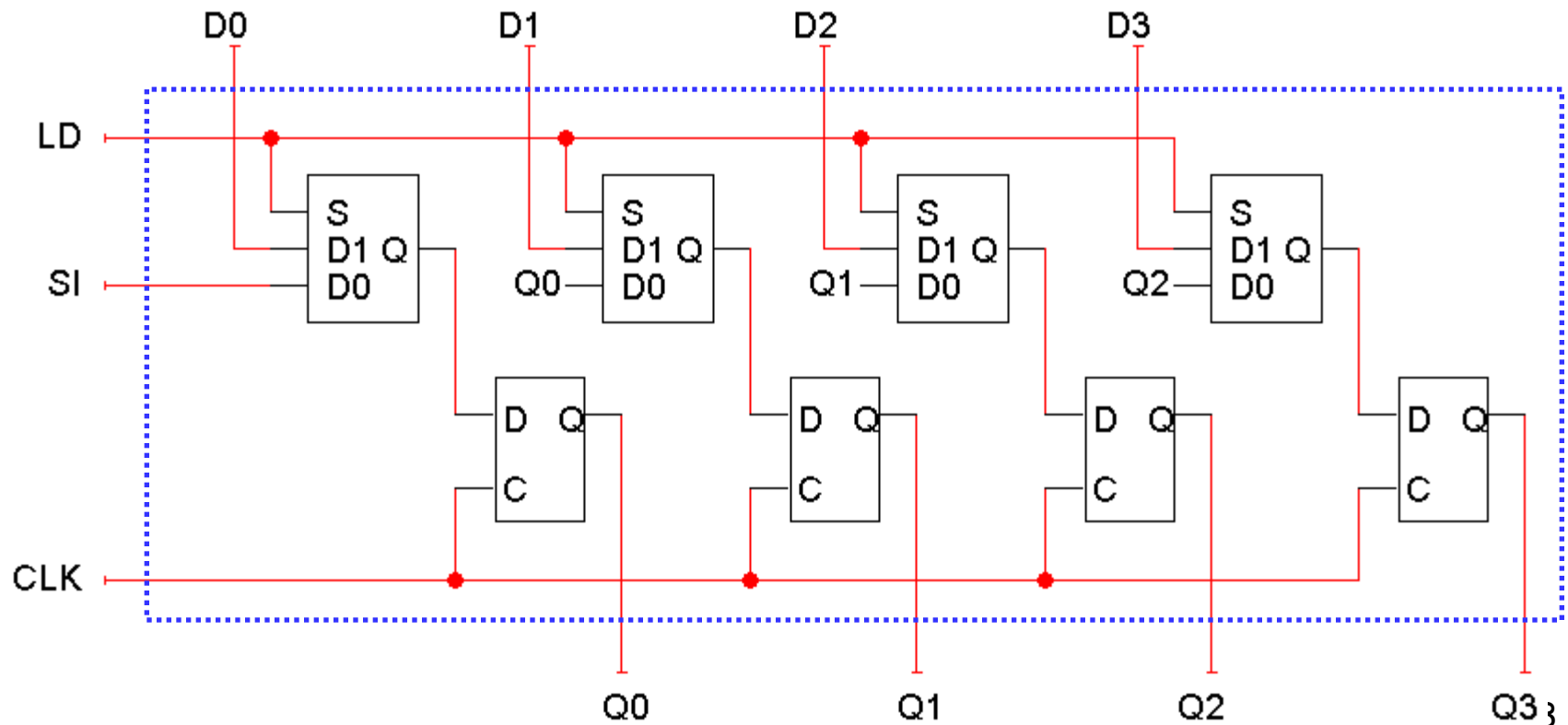
Present Q_0 - Q_3	SI	Next Q_0 - Q_3
ABCD	X	XABC

- But it really depends on your interpretation of the bits. If you consider Q_3 to be the most significant bit instead, then the register is shifting in the *opposite* direction!

Present Q_3 - Q_0	SI	Next Q_3 - Q_0
DCBA	X	CBAX

Shift register with parallel load

- We can add a parallel load, just like we did for regular registers
 - When $LD = 0$, the flip-flop inputs will be $SIQ_0Q_1Q_2$, so the register shifts on the next positive clock edge
 - When $LD = 1$, the flip-flop inputs are D_0-D_3 , and a new value is loaded into the shift register, on the next positive clock edge



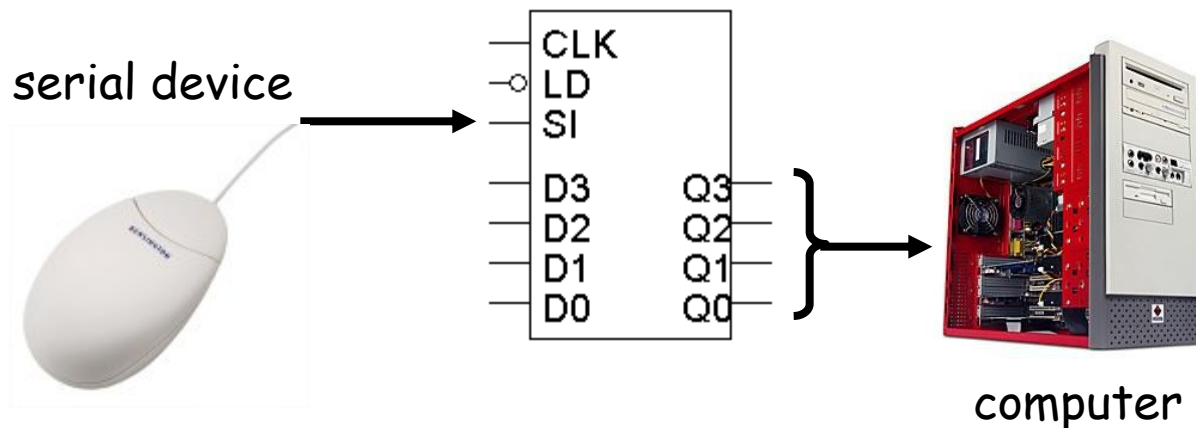
Serial data transfer

- One application of shift registers is converting between “serial data” and “parallel data”
- Computers typically work with multiple-bit quantities
 - ASCII text characters are 8 bits long
 - Integers, single-precision floating-point numbers, and screen pixels are up to 32 bits long
- But sometimes it's necessary to send or receive data **serially**, or one bit at a time. Some examples include:
 - Input devices such as keyboards and mice
 - Output devices like printers
 - Any serial port, USB or Firewire device transfers data serially
 - Recent switch from Parallel ATA to Serial ATA in hard drives



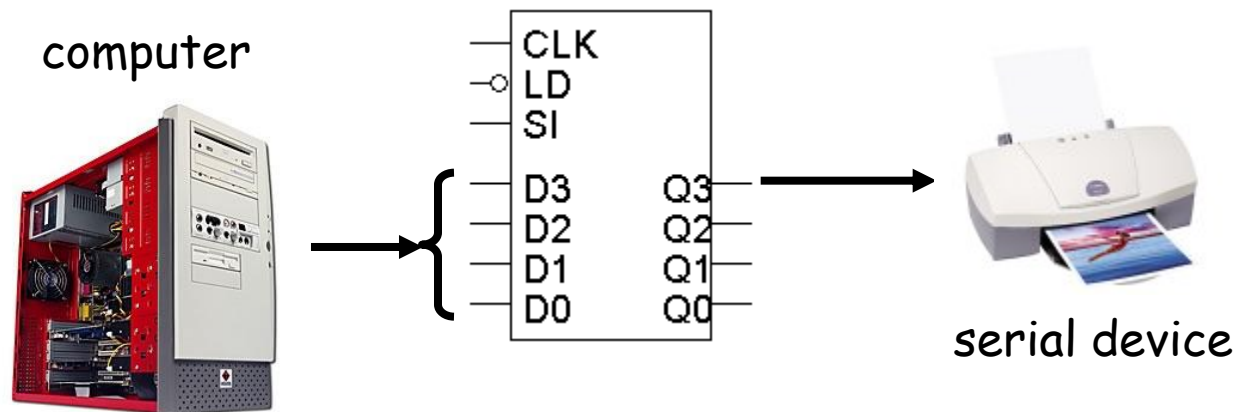
Receiving serial data

- To *receive* serial data using a shift register:
 - The serial device is connected to the register's SI input
 - The shift register outputs Q3-Q0 are connected to the computer
- The serial device transmits one bit of data per clock cycle
 - These bits go into the SI input of the shift register
 - After four clock cycles, the shift register will hold a four-bit word
- The computer then reads all four bits at once from the Q3-Q0 outputs.



Sending data serially

- To *send* data serially with a shift register, you do the opposite:
 - The CPU is connected to the register's D inputs
 - The shift output (Q3 in this case) is connected to the serial device
- The computer first stores a four-bit word in the register, in one cycle
- The serial device can then read the shift output
 - One bit appears on Q3 on each clock cycle
 - After four cycles, the entire four-bit word will have been sent



Registers in Modern Hardware

- Registers store data in the CPU
 - Used to supply values to the ALU
 - Used to store the results
- If we can use registers, why bother with RAM?

CPU	GPR's	Size	L1 Cache	L2 Cache
Pentium 4	8	32 bits	8 KB	512 KB
Athlon XP	8	32 bits	64 KB	512 KB
Athlon 64	16	64 bits	64 KB	1024 KB
PowerPC 970 (G5)	32	64 bits	64 KB	512 KB
Itanium 2	128	64 bits	16 KB	256 KB
MIPS R14000	32	64 bits	32 KB	16 MB

Answer: Registers are expensive!

- Registers occupy the most expensive space on a chip - the core
- L1 and L2 are very fast RAM - but not as fast as registers.

Registers summary

- A register is a special state machine that stores multiple bits of data
- Several variations are possible:
 - Parallel loading to store data into the register
 - Shifting the register contents either left or right
 - Counters are considered a type of register too!
- One application of shift registers is converting between serial and parallel data
- Most programs need more storage space than registers provide
 - We'll introduce RAM to address this problem
- Registers are a central part of modern processors