

MEASURES OF VARIABILITY

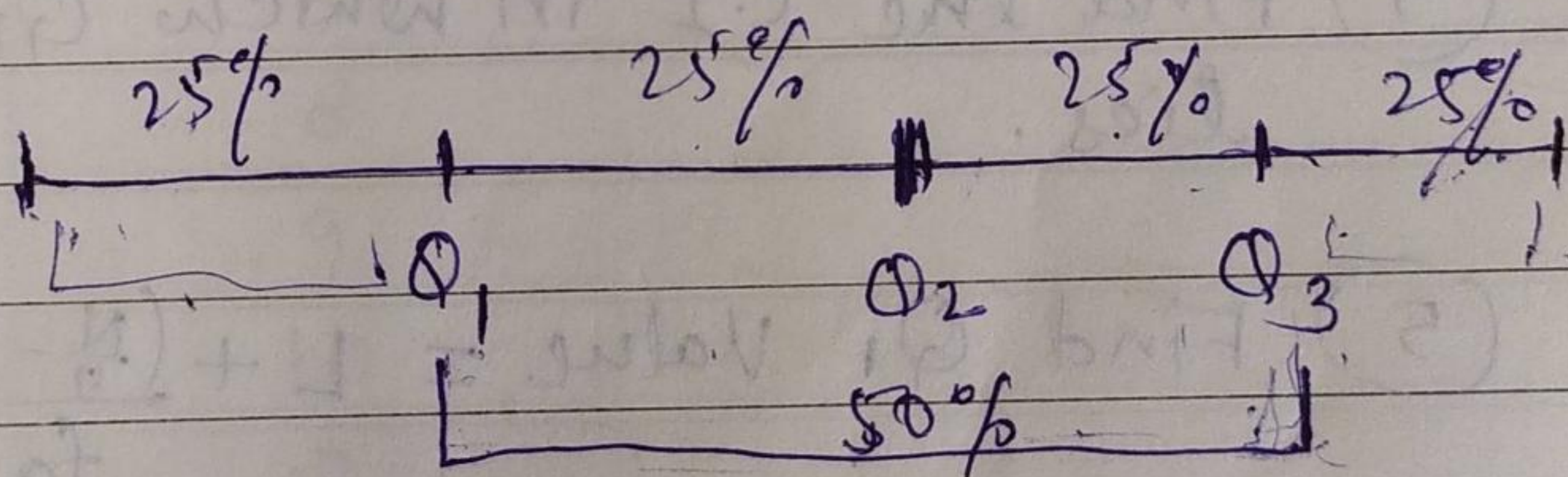
Quartile Deviation

चतुर्थांश विचलन

⇒ Improved form of Range
विस्तार विचलन का सुधरा हुआ रूप

⇒ Given importance to middle 50% scores.

मध्य के 50% अंकों को महत्व दिया जाता है।



⇒ Symbol denoted by 'Q'

⇒ Formula of Quartile Deviation

$$Q = \frac{Q_3 - Q_1}{2}$$

⇒ Also known as Semi Inter Quartile Range.
अर्ध-आन्तरिक चतुर्थांश विचलन

Calculation of Q.D. in Ungrouped data

Steps - (1) Arrange the data in ascending order.

(2) Find N

(3) Find $Q_1 \text{ term} = \frac{(N+1)}{4}$

(4) Find Q_1 value

(5) Find $Q_3 \text{ term} = 3\left(\frac{N+1}{4}\right)$

(6) Find Q_3 value

(7) Find $Q = \frac{Q_3 - Q_1}{2}$

Que. Find Q from the following data

(X) 6, 8, 10, 15, 7, 12, 13, 17, 21, 19, 18

Solution:-

Step (1) \rightarrow 6, 7, 8, 10, 12, 13, 15, 17, 18, 19, 21

Step (2) $\rightarrow N = 11$ (odd)

Step (3) $\rightarrow Q_1 \text{ term} = \frac{N+1}{4} = \frac{11+1}{4} = \frac{12}{4} = 3$

$Q_1 \text{ term} = 3^{\text{rd}} \text{ term}$

Step (4) $Q_1 \text{ value} = 8$

$$Q_1 = 8$$

Step (5) $Q_3 \text{ term} = 3\left(\frac{N+1}{4}\right) = 3 \times 3 = 9^{\text{th}} \text{ term}$

Step (6) $Q_3 \text{ value} = 18$

$$Q_3 = 18$$

Step (7)

$$Q = \frac{Q_3 - Q_1}{2}$$

$$= \frac{18 - 8}{2}$$

$$= \frac{10}{2}$$

$$Q = 5 \quad \text{Ans}$$

Ques Find Q

13, 18, 15, 8, 10, 19, 11, 20, 25, 22, 12, 16

Solution

step (1) 8, 10, 11, 12, 13, 15, 16, 18, 19, 20, 22, 25

step (2) $N = 12$ even

step (3) $Q_1 \text{ term} = \frac{N+1}{4} = \frac{12+1}{4} = \frac{13}{4} = 3.25 \text{ term}$

step (4) $Q_1 \text{ value} = 3\text{rd term} + 0.25 (4\text{th term} - 3\text{rd})$

(4th - 3rd) = 2.25

$$= 11 + 0.25(12 - 11)$$

$$= 11 + 0.25 \times 1$$

$$= 11 + 0.25$$

$$\boxed{Q_1 = 11.25}$$

step (5) $Q_3 \text{ term} = 3 \left(\frac{N+1}{4} \right) = 3 \times 3.25$

$Q_3 \text{ term} = 9.75 \text{ th term}$

step (6) $Q_3 \text{ value} = 9\text{th} + 0.75 (10\text{th} - 9\text{th})$

9.75 - 9 = 0.75

$$= 19 + 0.75(20 - 19)$$

$$= 19 + 0.75 \times 1$$

$$\boxed{Q_3 = 19.75}$$

step (7) $Q = \frac{Q_3 - Q_1}{2}$

$$= \frac{19.75 - 11.25}{2}$$

$$= \frac{8.50}{2}$$

$$\boxed{Q = 4.25} \text{ Ans}$$